# Mathematikal model of calculation parabola-cylindirical solar hot water systems of industrial enterprises

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#### Abstract

The article analyzes a mathematical model for calculating solar parabola cylindrical hot water systems for industrial and municipal enterprises. The formulas for determining heat losses associated with radiant and convective heat exchange, as well as useful heat energy and efficiency of solar parabolacylindrical systems for obtaining heat for industrial purposes are given.

**Keywords:** Solar radiation, energy, temperature, heat supply, process steam, productivity, battery, hot water, thermal energy, electricity, optical losses, heat losses, hot water supply, energy balance, industry

## 1. INTRODUCTION

Most solar parabola-cylindrical hot water systems for industrial and municipal enterprises operate according to the thermal model shown in Fig.1 and consist of the following main components: parabola-cylindrical collectors, accumulator tank, circulation pumps and hot water supply doubler 1, 2, 4, 5, 6. The system is provided with hot water with a temperature of 60÷100°C.

The hot water supply system is made according to a single-circuit scheme, i.e. the heated water in parabola-cylindrical collectors enters the hot water storage tank. Water from the Central water supply network enters the lower part of the battery tank, and hot water for technological processes are taken from the upper part of the tank. The system is protected from freezing by draining water from the collectors.

## 2. MAIN PART

When the water temperature falls below the required operating temperature for the technological process,  $T^m_{\ \ c}$  the DT doubler is turned on; this will warm up the water coming from the storage tank.

The system works as follows. Circulation of water through parabola-cylindrical collectors occurs if the equilibrium temperature  $T_{\infty}$  the absorbing surface of the heat receiver is higher than the temperature  $T_{E}$  at the bottom of the battery tank by the amount of  $\Delta T$  due to the temperature difference in the main pipelines of this circuit

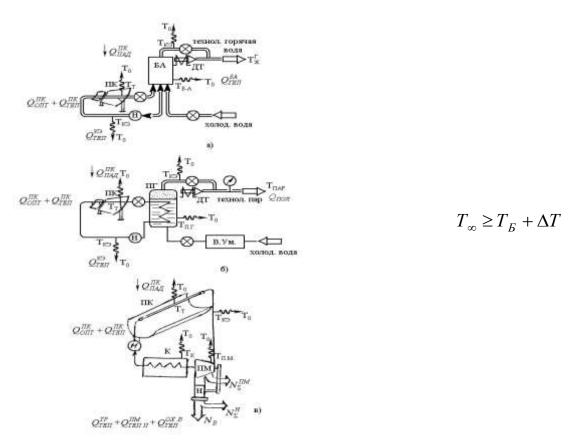


Fig. 1 Thermal models of parabola-cylindrical installations for the production of hot water (a), steam (b) and water lifting (C).

(1) Hot water is extracted from the upper part of the battery tank by the flow rate  $m_r$  to places where water is collected. From Fig.2 it can be seen that the consumption  $m_r$  defined as follows:

$$\begin{split} m_r &= m_{\Gamma}^T \quad T_B \leq T_{\Gamma}^T \\ &\text{and from the equality} \quad m_r \cdot C_P \cdot T_E + \left( m_{\Gamma}^T - m_r \right) C_P \cdot \tau_{x.s.} = m_{\Gamma}^T \cdot C_P \cdot T_{\Gamma}^T \\ &m_r = m_r^T \frac{\left( T_{\Gamma}^T - T_{x.s} \right)}{\left( T_E - T_{x.s} \right)} \quad T_E > T_{\Gamma}^T \end{split} \tag{2}$$

where:  $T_{\Gamma}^{T}$ ,  $m_{r}^{T}$  - water temperature and flow rate determined by the process load schedule;  $T_{x.8}$  - the temperature of the feed water provided from a Central water supply network. In the description of the mathematical model parabola-cylindrical hot

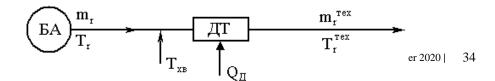


Fig. 2. Scheme for determining  $m_r$ 

the following assumptions were made: neglect the uneven distribution of solar energy flow between collectors; do not take into account heat loss from the surface of connecting pipelines; based on the results of preliminary calculations, neglect the temperature gradient along the perimeter and heat loss by thermal conductivity to the supporting elements of the heat receiver design. These assumptions make it possible to significantly simplify the mathematical model of the system, and consider parabolocylindric collectors as a single collector.

To consider the energy balance over time, the estimated period of operation of the system is divided into

N equal parts in increments  $\Delta \tau$ , for each  $\tau_i$  point in time  $\left(i=1,2,...N\right)$  at the beginning of the step, the thermal balance of each system element is considered. In this case, the main dependencies used for

calculating each component of the system at a time  ${}^{\mathcal{T}}{}_i$  and the functional relationship between the elements are shown below.

Unit parabola-cylindrical collectors. To determine the useful heat  $Q_{no\pi}^{n\kappa}$ , the collector energy balance equation is used for the energy received from the parabolocylindric collectors in the storage tank,

expressed in terms of the equilibrium temperature of the absorbing surface of the receiver  $T_{\infty}$  and

temperature 
$$T_B$$
 at the bottom of the tank  $Q_{no\pi}^{n\kappa} = F_3 \cdot F_R \cdot U_L \cdot C^{-1} (T_\infty - T_B)$ 

Equilibrium temperature  $T_{\infty}$  the absorption surface of the receiver is determined by the formula [7]

$$T_{\infty} = T_O + \frac{E_O \cdot \eta_O \cdot K_{3an} \cdot C}{U_L}, \tag{5}$$

where:  $K_{\scriptscriptstyle 3an}$  -coefficient that takes into account dust on the mirror surface of the hub.

When calculating the flow density of direct solar radiation, the main methods used are the orientation of collectors rotating around a horizontal North-South or East-West axis.

Heat losses associated with partial boiling and evaporation of water are determined by the formula [7]

$$Q_{ucn}^{nom.} = Q_{non}^{n\kappa} - m_{\kappa} \cdot C_P (T_u - T_E)$$
(6)

where:  $T_u$  - boiling point of water;

 $m_{\kappa}$  - water consumption in the system circuit.

The flow rate of evaporated water is determined by a well-known formula [8]:

$$m_u = Q_u / r$$

 $m_u - \mathcal{L}_{u} / r$ . (7) Taking into account (7) the water temperature at the outlet of the heat receiver is determined by the

$$T_{\kappa}^{\text{gbix}} = T_{E} + \frac{\left(Qnno - Q_{ucn}^{nom}\right)}{m_{\kappa}C_{P}}$$
(8

At the end time of the estimated period of operation of the system, the following values are determined that characterize the balance of water heating energy in parabola-cylindrical collectors:

 $(Q_{na\partial})_{\!\Sigma}$  on the collector surface 1. The Sum of the incident (direct component) of solar radiation perpendicular to the rays:

$$(Q_{na\partial})_{\Sigma} = \sum_{I=1}^{N} \left( E_{oi} \cdot F_3 \cdot \Delta \tau \cdot 10^{-3} \right)$$
(9)

2. Total solar energy  $(Q_{noz})_{\Sigma}$  absorbed in the collector's heat sink:

$$(Q_{no\varepsilon})_{\Sigma} = \sum_{I=1}^{N} (E_{oi} \cdot F_3 \cdot \eta_o \cdot \Delta \tau \cdot 10^{-3})$$
(10)

3. The total optical loss in parabola-cilindrical collectors

$$(Q_{onm}^{nom})_{\Sigma} = (Q_{na\partial})_{\Sigma} - (Q_{no\varepsilon})_{\Sigma}. \tag{11}$$

4. Solar energy  $Q_{noz}$ <sub>y,H</sub> water absorbed during the operation of the circulation pump through the collector. Value  $Q_{noz}$ <sub>y,H</sub> defined using equation (11) when the condition is met  $T_{\infty} \geq T_{E} + \Delta T$ .

5. Total amount of heat  $\left(Q_{non}^{n\kappa}\right)_{\Sigma}^{b}$  coming into the storage tank of parabola-cilindrical collectors

$$(Q_{non}^{n\kappa})_{\Sigma}^{E} = \sum_{i=1}^{N} Q_{non}^{n\kappa} \Delta \tau \cdot 10^{-3} = \sum_{i=1}^{N} [(m_{k} - m_{u})C_{P}(T_{\kappa}^{sbx} - T_{E}) \cdot \Delta \tau \cdot 10^{-3}]$$
 (19)

6. Heat losses in the collector heat sink  $Q_{men}^{nom}$  $_{HB}^{m.c}$  caused by the impossibility of heat removal by the heat carrier of the absorbed solar radiation under the condition  $T_{\infty} < T_{E} + \Delta T$ 

$$\left(Q_{men}^{nom}\right)_{HB}^{nc} = \left(Q_{noz}\right)_{\Sigma} - \left(Q_{noz}\right)_{\Sigma} - \left(Q_{noz}\right)_{u,H} \tag{20}$$

7. The total heat loss  $Q_{men}^{nom}$  taking into account heat loss  $Q_{men}^{nom}$  partially evaporated water at the rate of mu

$$(Q_{men}^{nom})_{\Sigma} = \sum_{i=1}^{N} [(m_{ui} \cdot C_P)(T_u - T_E) + (Q_{men}^{nom})_{ne.i}^{m.c}] \Delta \tau \cdot 10^{-3}$$
(21)

8. Heat losses in the collector during operation of the pump:

$$\left(Q_{men}^{nom}\right)_{u,H} = \left(Q_{nor}\right)_{u,H} - \left(Q_{non}^{n\kappa}\right)_{\Sigma}^{E} - \left(Q_{men}^{nom}\right)_{\Sigma}$$
(22)

The tank is a heat accumulator. To simplify the mathematical model of the heat storage tank, we write down the heat balance equation without taking into account stratification and heat loss from the tank surface [7, 8, 9].:

$$M_{E} \cdot F_{3} \cdot C_{P} \frac{dT_{E}}{d\tau} = (m_{k} - m_{u})C_{P} (T_{\kappa}^{Bblx} - T_{E}) + (m_{r} + m_{u})(T_{x.B} - T_{E})$$
(23)

where:  $M_{\it B}$  - mass of water in the accumulator tank per 1 m2 of the aperture area of the parabola-cylindrical collector, kg/m2

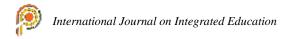
Integrating equation (23) according to the Euler model, we determine the temperatures  $T_{Ei+1}$  water at the end of the time step:

$$T_{Ei+1} = T_{E.i} + \frac{\Delta \tau}{M_E \cdot F_3} \left[ (m_k - m_u)(T_{ki} - T_{Ei}) + (m_{ri} + m_{ui})(T_{x.e} - T_{Ei}) \right]$$
(24)

backup in the load loop to the temperature  $T_{\Gamma}^{T}$  during the estimated period of operation of the system, it is determined by the formula:

$$\left(Q_{\mathcal{I}}\right)_{\Sigma} = \sum_{i=1}^{N} \left[ m_{\Gamma i}^{T} \cdot C_{P} \left(T_{\Gamma}^{T} - T_{E i}\right) \cdot \Delta \tau \cdot 10^{-3} \right]$$
(25)

Hot water supply load loop. Total amount of energy  $(Q_{H})_{\Sigma}$  the load that is diverted to the consumer with the water flow rate is determined by the following equation:



$$(Q_{\scriptscriptstyle H})_{\Sigma} = \sum_{i=1}^{N} \left[ m_{\Gamma}^{T} \cdot C_{P} \cdot \Delta \tau \left( T_{\Gamma}^{T} - T_{x.s} \right) \cdot 10^{-3} \right] = (Q_{\scriptscriptstyle H})_{cym} \cdot N_{\scriptscriptstyle 9}$$
(26)

where:  $(Q_{\scriptscriptstyle H})_{\scriptscriptstyle {\it cym}}$  - daily heat load of hot water supply, kWh / day;

 $N_9$  - the number of days of operation of the system during the period of operation, day/year In addition, at the end time, the total amount of solar heat received by the load from the system and provided by the use of solar energy is determined.

$$(Q_c)_{\Sigma} = \sum_{i=1}^{N} \left[ m_r \cdot C_P (T_B - T_{x.e}) \Delta \tau \cdot 10^{-3} \right]$$

(27)

# 3. CONCLUSION

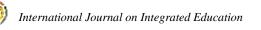
Thus, according to the above formulas, the energy indicators of solar parabola-cylindrical hot water systems of industrial and municipal enterprises can be determined

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